

Cambridge International A Level

MATHEMATICS
Paper 3 Pure Mathematics 3
May/June 2020
MARK SCHEME
Maximum Mark: 75

Published

Students did not sit exam papers in the June 2020 series due to the Covid-19 global pandemic.

This mark scheme is published to support teachers and students and should be read together with the question paper. It shows the requirements of the exam. The answer column of the mark scheme shows the proposed basis on which Examiners would award marks for this exam. Where appropriate, this column also provides the most likely acceptable alternative responses expected from students. Examiners usually review the mark scheme after they have seen student responses and update the mark scheme if appropriate. In the June series, Examiners were unable to consider the acceptability of alternative responses, as there were no student responses to consider.

Mark schemes should usually be read together with the Principal Examiner Report for Teachers. However, because students did not sit exam papers, there is no Principal Examiner Report for Teachers for the June 2020 series.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the June 2020 series for most Cambridge IGCSE™ and Cambridge International A & AS Level components, and some Cambridge O Level components.

This document consists of 13 printed pages.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

© UCLES 2020 Page 2 of 13

May/June 2020

Ma	athematics Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct marks will be awarded for a scale drawing.	ethod. However, if a calculation is required then no
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore su is not affected.	perfluous zeros, provided that the degree of accuracy
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being use	ed as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a	a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provide method required, award all marks earned and deduct just 1 mark for the misread.	led that number does not alter the difficulty or the
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working	ng makes the candidate's intent clear.

© UCLES 2020 Page 3 of 13

Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

© UCLES 2020 Page 4 of 13

May/June 2020

Abbreviations

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only

ISW Ignore Subsequent Working

SOI Seen Or Implied

SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the

light of a particular circumstance)

WWW Without Wrong Working

AWRT Answer Which Rounds To

© UCLES 2020 Page 5 of 13

Question	Answer	Marks
1	Commence division and reach partial quotient $3x^2 + kx$	M1
	Obtain quotient $3x^2 + 2x - 1$	A1
	Obtain remainder $2x - 5$	A1
		4

Question	Answer	Marks
2	State or imply $2 \ln y = \ln A + kx$	B1
	Substitute values of $\ln y$ and x , or equate gradient of line to k , and solve for k	M1
	Obtain $k = 0.80$	A1
	Solve for ln A	M1
	Obtain $A = 3.31$	A1
	Alternative method for question 2	
	Obtain two correct equations in y and x by substituting y- and x- values in the given equation	B1
	Solve for k	M1
	Obtain $k = 0.80$	A1
	Solve for A	M1
	Obtain $A = 3.31$	A1
		5

© UCLES 2020 Page 6 of 13

Question	Answer	Marks
3	Commence integration and reach $ax^{\frac{5}{2}} \ln x + b \int x^{\frac{5}{2}} \cdot \frac{1}{x} dx$	M1*
	Obtain $\frac{2}{5}x^{\frac{5}{2}}\ln x - \frac{2}{5}\int x^{\frac{5}{2}} \cdot \frac{1}{x} dx$	A1
	Complete the integration and obtain $\frac{2}{5}x^{\frac{5}{2}}\ln x - \frac{4}{25}x^{\frac{5}{2}}$, or equivalent	A1
	Use limits correctly, having integrated twice e.g $\frac{2}{5} \times 32 \ln 4 - \frac{4}{25} \times 32 - \left(\frac{2}{5} \times 0\right) + \frac{4}{25}$	DM1
	Obtain answer $\frac{128}{5} \ln 2 - \frac{124}{25}$, or exact equivalent	A1
		5

Question	Answer	Marks
4	Use correct product rule	M1
	Obtain correct derivative in any form, e.g. $-\sin x \sin 2x + 2\cos x \cos 2x$	A1
	Use double angle formula to express derivative in terms of $\sin x$ and $\cos x$	M1
	Equate derivative to zero and obtain an equation in one trig function	M1
	Obtain $3 \sin 2x = 1$, or $3 \cos 2x = 2$ or $2 \tan 2x = 1$	A1
	Solve and obtain $x = 0.615$	A1
		6

Question	Answer	Marks
5(a)	State $R = \sqrt{7}$	B1
	Use trig formulae to find $lpha$	M1
	Obtain $\alpha = 57.688^{\circ}$	A1
		3
5(b)	Evaluate $\cos -1\left(\frac{1}{\sqrt{7}}\right)$ to at least 3 d.p. (67.792°) (FT is on their R)	B1 FT
	Use correct method to find a value of θ in the interval	M1
	Obtain answer, e.g. 5.1°	A1
	Obtain second answer, e.g.117.3°, only	A1
		4

6(a)	Use quotient or product rule	M1
	Obtain correct derivative in any form e.g. $\frac{(1+3x^4)-x\times12x^3}{(1+3x^4)^2}$	A1
	Equate derivative to zero and solve for <i>x</i>	M1
	Obtain answer 0.577	A1
		4

9709/32

Question	Answer	Marks
6(b)	State or imply $du = 2\sqrt{3x} dx$, or equivalent	B1
	Substitute for x and dx	M1
	Obtain integrand $\frac{1}{2\sqrt{3(1+u^2)}}$, or equivalent	A1
	State integral of the form $a \tan^{-1} u$ and use limits $u = 0$ and $u = \sqrt{3}$ (or $x = 0$ and $x = 1$) correctly	M1
	Obtain answer $\frac{\sqrt{3}}{18}\pi$, or exact equivalent	A1
		5

Question	Answer	Marks
7	Separate variables correctly and integrate at least one side	B1
	Obtain term $ln(y-1)$	B1
	Carry out a relevant method to determine A and B such that $\frac{1}{(x+1)(x+3)} = \frac{A}{x+1} + \frac{B}{x+3}$	M1
	Obtain $A = \frac{1}{2}$ and $B = -\frac{1}{2}$	A1
	Integrate and obtain terms $\frac{1}{2}\ln(x+1) - \frac{1}{2}\ln(x+3) = \frac{1}{2}\ln(x+1) - \frac{1}{2}\ln(x+3)$, or equivalent (FT is on A and B)	A1 FT + A1 FT
	Use $x = 0$, $y = 2$ to evaluate a constant, or as limits in a solution containing terms of the form $a \ln(y - 1)$, $b \ln(x + 1)$ and $c \ln(x + 3)$, where $abc \neq 0$	M1
	Obtain correct answer in any form	A1
	Obtain final answer $y = 1 + \sqrt{\frac{3x+3}{x+3}}$, or equivalent	A1
		9

Question	Answer	Marks
8(a)	Substitute and obtain a correct equation in x and y	B1
	Use $i^2 = -1$ and equate real and imaginary parts	M1
	Obtain two correct equations in x and y, e.g. $x-y=3$ and $3x+y=5$	A1
	Solve and obtain answer $z = 2 - i$	A1
		4
8(b)(i)	Show a point representing 2 + 2i	B1
	Show a circle with radius 1 and centre not at the origin (FT is on the point representing the centre)	B1 FT
	Show the correct half line from 4i	B1
	Shade the correct region	B1
		4
8(b)(ii)	Carry out a complete method for finding the least value of Im z	M1
	Obtain answer $2 - \frac{1}{2}\sqrt{2}$, or exact equivalent	A1
		2

Question	Answer	Marks
9(a)	State $\cos p = \frac{k}{1+p}$	B1
	Differentiate both equations and equate derivatives at $x = p$	M1
	Obtain a correct equation in any form, e.g. $-\sin p = -\frac{k}{(1+p)^2}$	A1
	Eliminate <i>k</i>	M1
	Obtain the given answer showing sufficient working	A1
		5
9(b)	Use the iterative formula correctly at least once	M1
	Obtain final answer $p = 0.568$	A1
	Show sufficient iterations to justify 0.568 to 3 d.p., or show there is a sign change in the interval (0.5675, 0.5685)	A1
		3
9(c)	Use a correct method to find k	M1
	Obtain answer $k = 1.32$	A1
		2

9709/32

Question	Answer	Marks
10(a)	State that the position vector of M is $3\mathbf{i} + \mathbf{j}$	B1
	Use a correct method to find the position vector of N	M1
	Obtain answer $\frac{10}{3}$ i + 2 j + 2 k	A1
	Use a correct method to form an equation for MN	M1
	Obtain correct answer in any form, e.g. $\mathbf{r} = 3\mathbf{i} + \mathbf{j} + \lambda \left(\frac{1}{3}\mathbf{i} + \mathbf{j} + 2\mathbf{k} \right)$	A1
		5
10(b)	State or imply $\mathbf{r} = \mu(2\mathbf{i} + 2\mathbf{j} + 3\mathbf{k})$ as equation for <i>OB</i>	B1
	Equate sufficient components of MN and OB and solve for λ or for μ	M1
	Obtain $\lambda = 3$ or $\mu = 2$ and position vector $4\mathbf{i} + 4\mathbf{j} + 6\mathbf{k}$ for P	A1
		3
10(c)	Carry out correct process for evaluating the scalar product of direction vectors for <i>OP</i> and <i>MP</i> , or equivalent	M1
	Using the correct process for the moduli, divide the scalar product by the product of the moduli and evaluate the inverse cosine of the result	M1
	Obtain answer 21.6°	A1
		3